

Paper : Physical Chemistry

Topic : Chemical Kinetics

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## Second Order Reactions

The rate of second order reactions is proportional to the square of concentration of one reactant - or product - of concentrations of two reactants having power unity. i.e.

$$\text{Rate} = k [A]^2$$

or  $\text{Rate} = k [A][B]$

Here we see that (i) the rate depends on two variable concentration terms which may or may not be same and (ii) the rate increases by  $n^2$  times if concentration of reactants is increased by  $n$  times.

For a second order reaction, there may be two cases:

- (a) when concentrations of reactants are same, and  
 (b) when concentrations of reactants are different. Now,

(a) When Concentrations of Reactants are Same :-

Consider the following second order reactions



$$\text{at } t=0 \quad a \quad 0$$

$$\text{at } t=t \quad (a-x) \quad x$$



$$\text{at } t=0 \quad a \quad a \quad 0$$

$$\text{at } t=t \quad (a-x) \quad (a-x) \quad x$$

$$\text{So, Rate} = \frac{dx}{dt} = k(a-x)^2 \quad \text{--- (1)}$$

On rearranging this equation we have

$$\frac{dx}{(a-x)^2} = k \cdot dt$$

On integration it gives

$$\frac{1}{(a-x)} = kt + I \quad \text{--- (2)}$$

where  $I$  is integration constant. The value of  $I$  can be determined by putting  $t=0$  and  $x=0$ . Thus

$$I = \frac{1}{a}$$

Substituting for  $I$  in equation (2) we get

$$\frac{1}{(a-x)} = kt + \frac{1}{a}$$

$$\text{or } k \cdot t = \frac{1}{(a-x)} - \frac{1}{a}$$

$$\text{or } k = \frac{1}{t} \cdot \frac{x}{a(a-x)} \quad \text{--- (3)}$$

This is the integrated rate equation for a second order reaction.

(b.) When Concentrations of Reactants are Different : —

Consider the following second order reaction starting with different initial concentrations of reactants



$$\text{at } t=0 \quad a \quad b \quad 0$$

$$\text{at } t=t \quad (a-x) \quad (b-x) \quad x$$

$$\text{and Rate} = \frac{dx}{dt} = k(a-x)(b-x) \quad \text{--- (1)}$$

After rearranging this we get

$$\frac{dx}{(a-x)(b-x)} = k \cdot dt \quad \text{--- (2)}$$

again using "partial fractions" <sup>(\*)</sup> we get-

$$\frac{1}{(a-b)} \left[ \frac{dx}{(b-x)} - \frac{dx}{(a-x)} \right] = k \cdot dt \quad \text{--- (3)}$$

By integrating this equation we get-

$$\frac{1}{(a-b)} \left[ -\ln(b-x) + \ln(a-x) \right] = kt + I \quad \text{--- (4)}$$

$$\text{or } \frac{1}{(a-b)} \left[ \ln \frac{(a-x)}{(b-x)} \right] = kt + I \quad \text{--- (5)}$$

The integration constant- I can be evaluated by putting  $t=0$  and  $x=0$ , then

$$I = \frac{1}{(a-b)} \left[ \ln \frac{a}{b} \right]$$

Substituting the value of I in equation (5) we get

$$\frac{1}{(a-b)} \left[ \ln \frac{(a-x)}{(b-x)} \right] = kt + \frac{1}{(a-b)} \left[ \ln \frac{a}{b} \right]$$

$$\text{or, } kt = \frac{1}{(a-b)} \left[ \ln \frac{(a-x)}{(b-x)} - \ln \frac{a}{b} \right]$$

$$\text{or, } k = \frac{1}{t(a-b)} \left[ \ln \frac{b(a-x)}{a(b-x)} \right] \quad \text{--- (6)}$$

$$\text{or } k = \frac{2.303}{t(a-b)} \log \frac{b(a-x)}{a(b-x)} \quad \text{--- (7)}$$

Equations (6) and (7) are the integrated rate equation for second order reaction.

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\* Partial Fraction:- The term

$\frac{1}{(a-x)(b-x)}$  can be broken into partial fraction as shown below

$$\frac{1}{(a-x)(b-x)} = \frac{A}{(a-x)} + \frac{B}{(b-x)}$$

$$\text{or } A(b-x) + B(a-x) = 1$$

$$\text{If } x = a, \text{ then } A(b-a) = 1$$

$$\text{or, } A = \frac{1}{(b-a)}$$

$$\text{If } x = b, \text{ then } B(a-b) = 1$$

$$\text{or, } B = \frac{1}{(a-b)}$$

On putting the values of A and B in above equation we have

$$\begin{aligned} \frac{1}{(a-x)(b-x)} &= \frac{1}{(b-a)(a-x)} + \frac{1}{(a-b)(b-x)} \\ &= \frac{1}{(a-b)} \left[ \frac{1}{(b-x)} - \frac{1}{(a-x)} \right] \end{aligned}$$


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Units of Second Order Rate Constant:-

The rate constant for a second order reaction is expressed as

$$k = \frac{1}{t} \times \frac{x}{a(a-x)}$$

$$= \frac{1}{\text{time}} \times \frac{\text{concentration}}{\text{Concentration} \times \text{Concentration}}$$

$$= \frac{1}{\text{time}} \times \frac{1}{\text{concentration}}$$

$$= \frac{1}{\text{second}} \times \frac{1}{\text{moles/litre}}$$

$$= \text{litre/mole/second}$$

∴ Units of  $k \Rightarrow \text{L} \cdot \text{mol}^{-1} \text{s}^{-1}$   
for second order  
reaction

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